

Shading

Course web page:

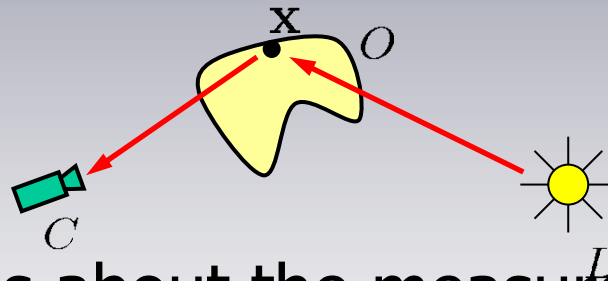
<http://goo.gl/EB3aA>

Outline

- Radiometry
- Surface properties
 - Diffuse/matte/Lambertian
 - Specular
- Simplified local model

Shading

- Geometry of perspective projection explains location of scene point in image, but what about its intensity and color?



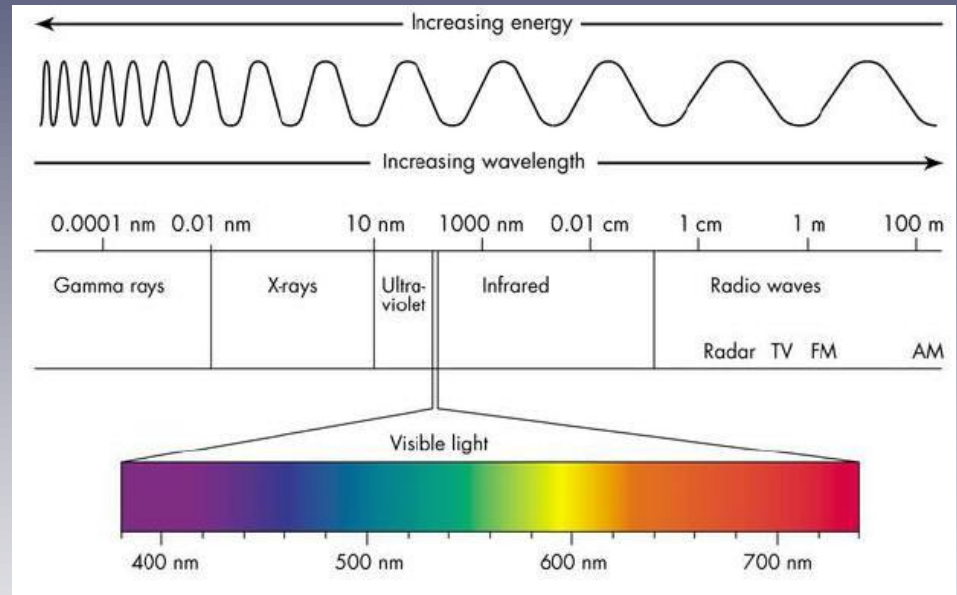
- **Radiometry** is about the measurement of electromagnetic radiation, in this case optical (Shirley, Chap. 20-20.2)
- **Photometry** quantifies camera/eye sensitivity (Shirley Chap. 20.3)

Lighting Objects



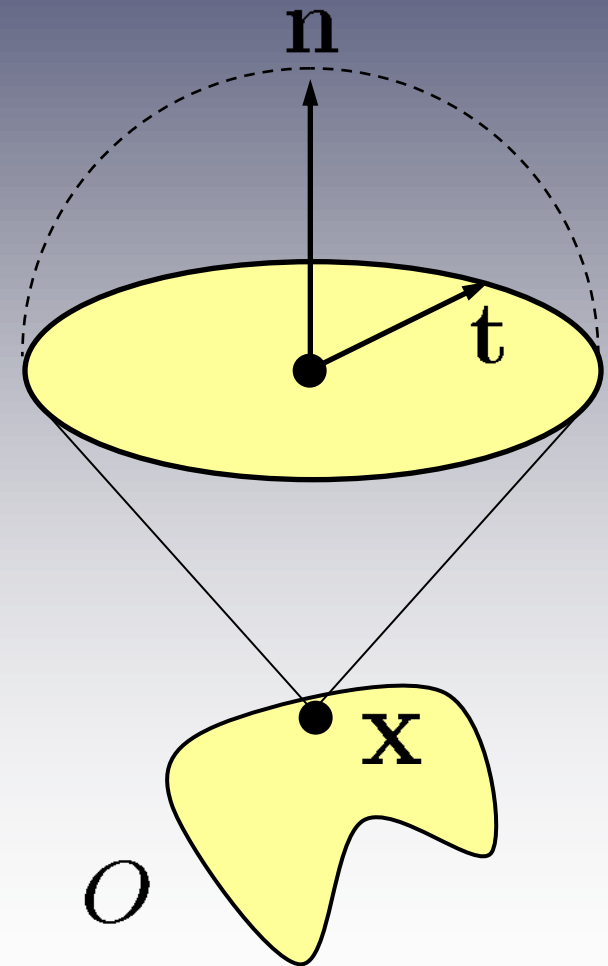
What is Light?

- A *photon* is a quantum of light with a:
 - 3-D position
 - 3-D direction of propagation
 - Wavelength λ
- *Energy* q carried by one photon is proportional to $1/\lambda$
- *Power* is energy per unit of time; units are watts W
- *Spectral power* is watts per unit of wavelength
 - In the following slides this is the kind of power we are talking about unless otherwise noted

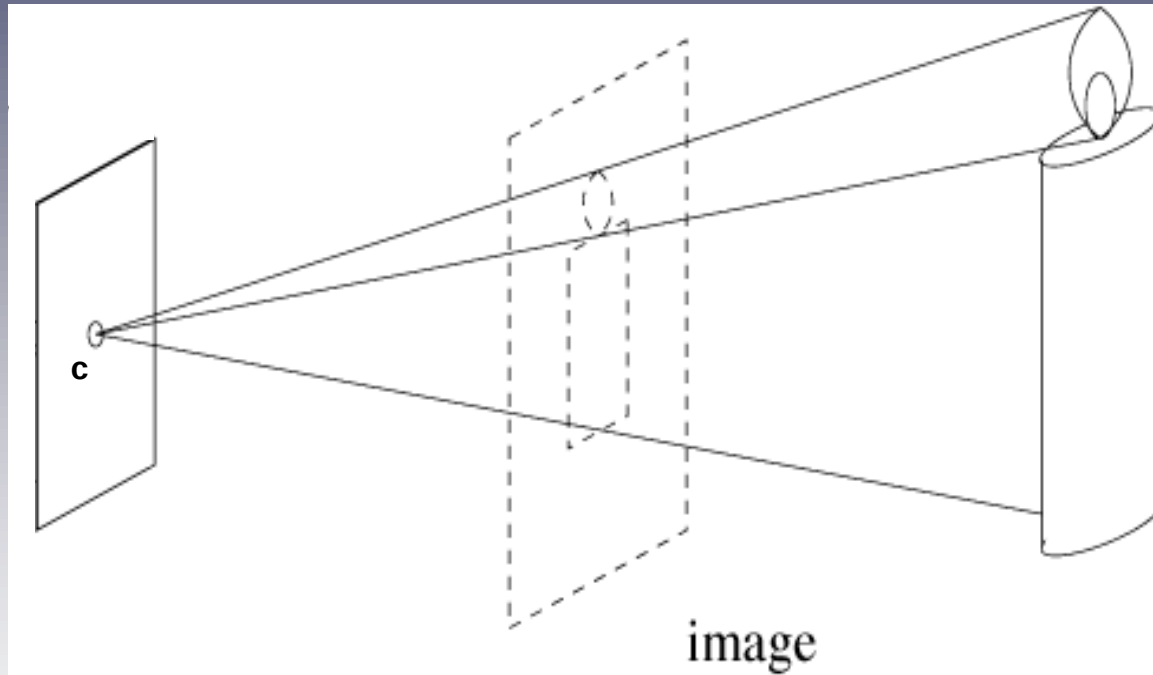


Incoming and Outgoing Light at a Surface

- **Irradiance** E (Wm^{-2})
 - Light power (watts) arriving at a point on a surface from all visible directions
 - An image samples the irradiance at the pinhole
 - Book uses variable H
- **Radiosity** B (Wm^{-2})
 - Light leaving a surface in all directions (per patch)
 - Also called “radiant exitance”



Perspective Projection



from Forsyth & Ponce

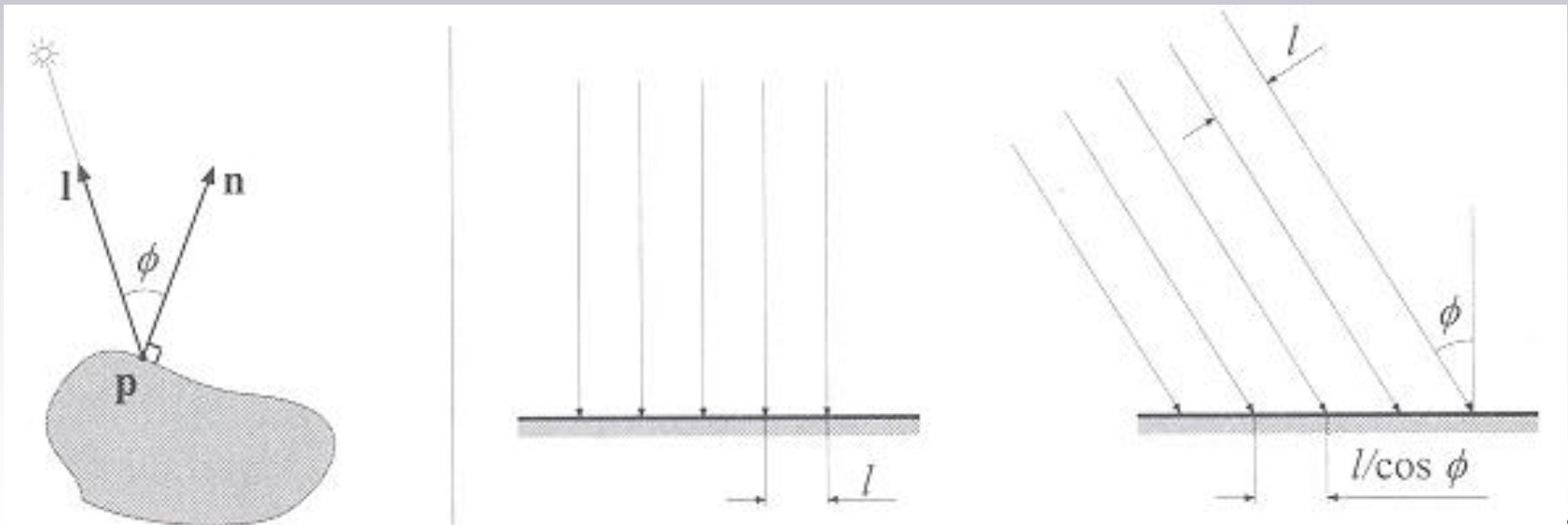
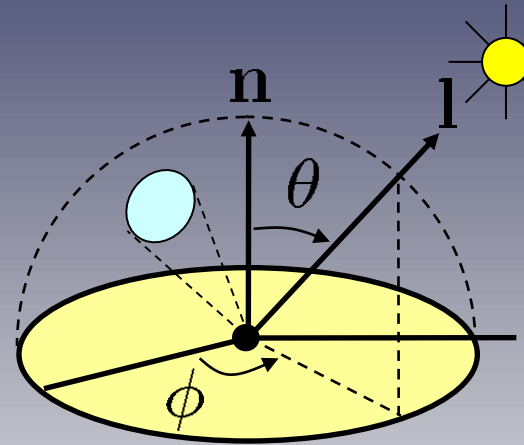
Instead of single direction **d** characteristic of parallel projections, rays emanating from single point **c** define perspective projection

Radiance

- Irradiance doesn't tell us **where** light came from
- **Radiance** L ($\text{Wm}^{-2}\text{sr}^{-1}$)
 - Power at a point in space in a given direction, per solid angle, foreshortened
 - Can be incoming or outgoing
 - Does not attenuate with distance in vacuum
- What is stored in **one** pixel—the light energy arriving along a particular ray at a particular point
 - After photometric considerations

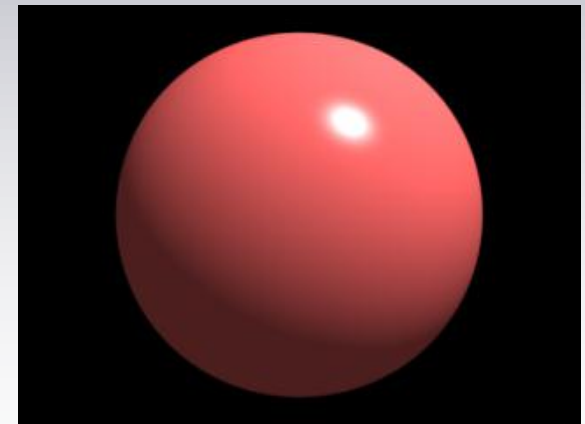
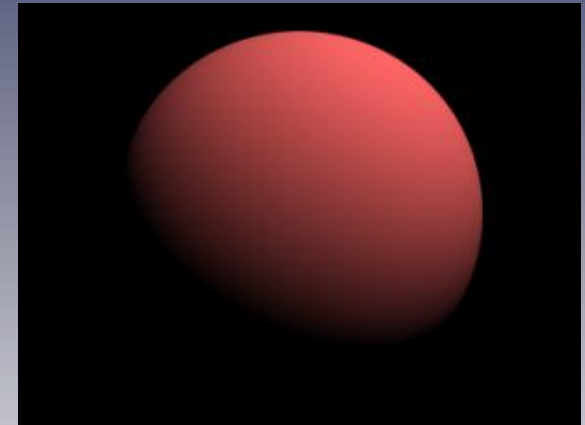
Foreshortening

- The more a surface is tilted away, the larger the area light energy is distributed over (and therefore is “diluted”)
 - In 2-D, received intensity is proportional to **cosine** of angle between light direction ***l*** and surface normal ***n***
 - Received intensity is greatest when ***l*** and ***n*** are parallel
- 3-D foreshortening factor for light coming from direction (θ, ϕ) is $\cos \theta$



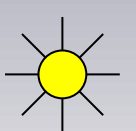
Object surface properties

- General
 - Light/dark/color
 - Reflectivity (e.g., matte/Lambertian vs. shiny)
- Space-varying pattern
 - I.e., are above characteristics different in different locations?
 - We'll get to this when we cover texture-mapping



Capturing Surface Properties: BRDF

- **Bidirectional Reflectance Distribution Function** (BRDF): Ratio of outgoing radiance in one direction to incident irradiance from another

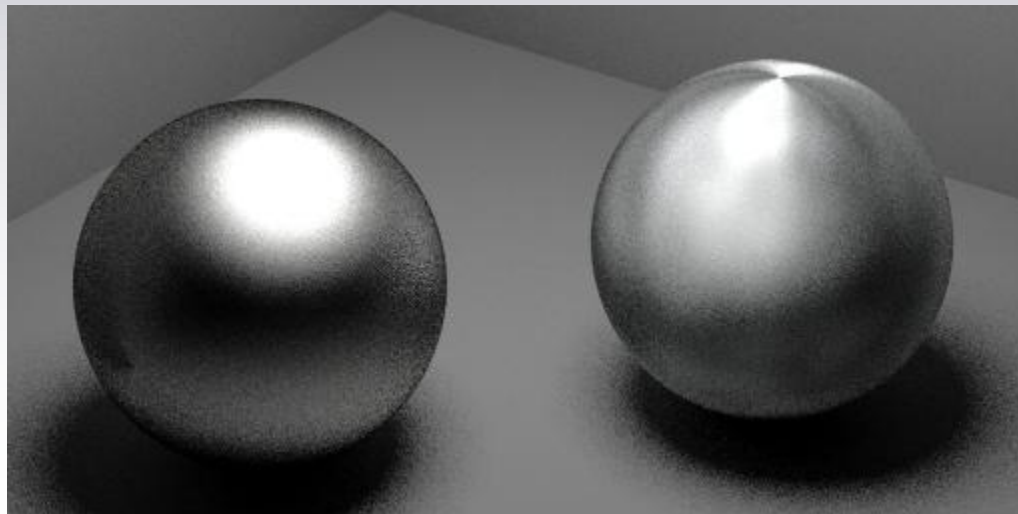


The diagram shows a yellow elliptical surface representing a plane. A vertical vector $\mathbf{n}$ represents the surface normal. An incident ray, labeled (θ_i, ϕ_i) , points towards the center of the surface. An outgoing ray, labeled (θ_o, ϕ_o) , points away from the center. The angle θ is the polar angle between the normal $\mathbf{n}$ and the outgoing ray. The angle ϕ is the azimuthal angle between the projection of the outgoing ray onto the surface and a reference axis. Dashed lines indicate the projection of the rays onto the surface plane.

$$f(\theta_o, \phi_o, \theta_i, \phi_i) = \frac{L(\theta_o, \phi_o)}{dE(\theta_i, \phi_i)}$$

BRDF Properties

- Energy leaving $\leq$ Energy arriving (**albedo** is fraction reflected)
- For a perfectly diffuse/Lambertian surface, the BRDF is a constant—incoming light is scattered equally in all directions
- Generally, only the **difference** between incident and emitted angle Φ (as well as polar angles) is significant
 - Dependence on absolute $\Phi \rightarrow$ *Anisotropy* (e.g., brushed metal, fur)



Reflectance equation

- Radiance for a viewing direction given all incoming light (also called *rendering* equation in Shirley 20.2):

$$L_o(\mathbf{x}, \theta_o, \phi_o) = \int_{\Omega} f(\theta_o, \phi_o, \theta_i, \phi_i) L_i(\mathbf{x}, \theta_i, \phi_i) \cos \theta_i d\omega$$

- This is expensive to compute in general, so the standard local approach is approximation:
 - Approximate incoming light as **ambient** (whole hemisphere) + set of point light sources
 - Approximate BRDF of surface as combination of **diffuse** (matte) and **specular** (shiny) factors

Illumination models

- Interaction between light sources and objects in scene that results in perception of intensity and color at eye
- **Local** vs. **global** models
 - Local illumination: Perception of a particular primitive only depends on light sources **directly** affecting that one primitive
 - Geometry
 - Material properties
 - Global illumination: Also take into account **indirect** effects on light of other objects in the scene
 - Shadows cast
 - Light reflected/refracted
 - More when we get to ray tracing